



DISCLAIMER:

PTAC does not warrant or make any representations or claims as to the validity, accuracy, currency, timeliness, completeness or otherwise of the information contained in this report, nor shall it be liable or responsible for any claim or damage, direct, indirect, special, consequential or otherwise arising out of the interpretation, use or reliance upon, authorized or unauthorized, of such information.

The material and information in this report are being made available only under the conditions set out herein. PTAC reserves rights to the intellectual property presented in this report, which includes, but is not limited to, our copyrights, trademarks and corporate logos. No material from this report may be copied, reproduced, republished, uploaded, posted, transmitted or distributed in any way, unless otherwise indicated on this report, except for your own personal or internal company use.

Emissions of Nitrogen Oxides from Turbulent Non-Premixed Flames: A Comparison to Current Emission Factors and Scaling Laws

A. Melina Jefferson^{*}, Darcy J. Corbin, Matthew R. Johnson[†]
*Energy and Emissions Research Laboratory, Carleton University
1125 Colonel By Drive, Ottawa, ON, K1S 5B6*

Abstract

Emission of nitrogen oxides (NO_x, sum of nitric oxide and nitrogen dioxide) were measured from turbulent non-premixed flames of pure propane and methane, and an alkane mixture of C1-C4. Results were compared with currently accessible emission factors and source data from governmental agencies in Canada, the United States, South America, and Europe. The linear relationship between NO_x emissions and mass, volume, and energy content of flare gas inherently assumed in available emission factors generally matched the trends in the current data, but variations in fuel composition could lead to an underestimation of emissions. NO_x emissions were underestimated by up to 24% from methane flames when using a mass-based emission factor, by up to 54% from propane flames using a volume-based factor, and by up to 12% for methane flames using a heat-release-based factor. A theoretical non-linear relationship between NO_x emission and volume flow rate parameters from the literature was examined and found to perform no better than the linear relations of current emission factors. A significant expansion of experimental data and conditions is required to fully comprehend the complexities of NO_x formation in non-premixed turbulent flames, and to the develop a robust NO_x emissions models necessary for gas flares used in the energy industry.

1. Introduction

Flaring is the practice of combusting unwanted or uneconomically viable flammable gases and is common in a multitude of industries. Recent satellite data suggest that approximately 140 billion cubic meters of gas are flared annually, amounting to 4% of global natural gas production [1,2]. Regulations in the United States and Canada for the upstream oil and gas industry promote flaring over venting as a means to reducing greenhouse gas emissions [3,4]. However, combustion emissions are still of concern. In addition to carbon dioxide emissions (CO₂), small quantities of unburned or partially combusted fuel (i.e. volatile organic compounds, VOCs) and criteria pollutants like carbon monoxide (CO), nitrogen oxides (NO_x), sulfur oxides (SO_x, in the case of sour gas), and black carbon (BC, a component of soot) may be emitted. These species have significant human health and environmental impacts: NO_x and SO_x lead to acid rain [5]; VOCs, NO_x, and soot promote the production of smog and ground-level ozone [5]; and BC is linked to respiratory illnesses and fatality [6]. Quantifying emission factors for these combustion products is vital to understanding the affect flaring has on the global climate and human health. Independent studies of wide ranges of fuels, flow, and flame regimes to determine robust NO_x emission factors are critically lacking – the focus of this paper is to compare experimental yields of NO_x with available emission factors and scaling laws to determine their applicability to a variety of flow conditions and fuels.

1.1 NO_x Emission Factors for Flaring

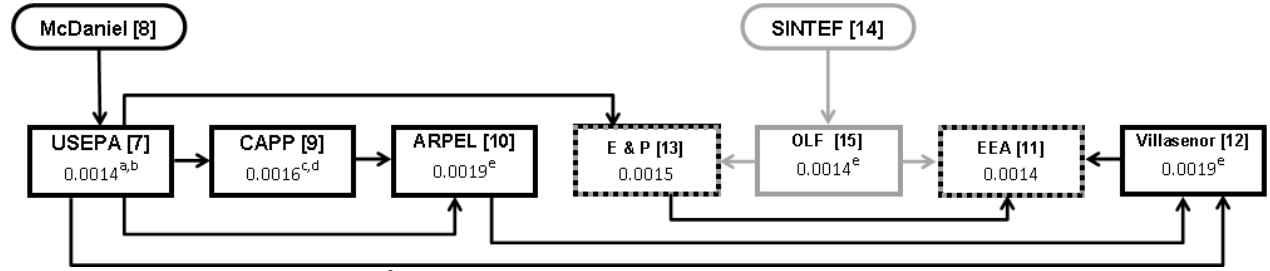
Current emission factors used or suggested by governmental agencies are single-value parameters linearly relating the mass emissions of NO_x to the mass, volume, or energy of the flare gas. The USEPA provides an emission factor of 0.068 lb NO_x per 10⁶ BTU of gas flared [7]. Available documentation indicates that this value is based upon a single study conducted in 1983 on a large-scale flare of crude propylene (80% propylene, 20% propane) [8].

The Canadian Association of Petroleum producers (CAPP) suggests an emission factor of 1.345 kg NO_x per 10³ m³ of fuel flared which is based exclusively on the emission factor from the USEPA using assumed heating value of 45 MJ/m³ [7,9]. In South America, ARPEL (Regional Association of Oil, Gas and Biofuels Sector Companies in Latin America and the Caribbean) published a report co-written by a Canadian environmental consulting agency with funding from the Canadian International Development Agency, suggesting an emission factor based upon [9] and [7]

^{*}Student presenter

[†]Professor, corresponding author, matthew.johnson@carleton.ca

of 0.0016 kg NO_x per m³ sweet gas [10]. In Europe, the EEA suggests a factor of 1.4 kg NO_x per metric ton of flare gas (sour, upstream oil and gas extraction flared specifically) [11], which was calculated using three reports: Villasenor et al. [12], a 1994 study by the Oil Industry International Exploration and Production Forum (E&P) [13], and a report by the Foundation for Scientific and Industrial Research (SINTEF) commissioned by the Norwegian Oil and Gas Industry (OLF) [14,15]. The factor proposed by [12] is the geometric mean of emission factors from [7] and [10] and [13] references emission factors from [7] and [14]. [14] re-analyzed data available in the literature and conducted field experiments on two off-shore flares to determine an emission factor of 1.2 kg NO_x per 10³ m³ flare gas. Figure 1 summarizes the web of references for each emission factor discussed. There are essentially only two sources of measurement data for the myriad available emission factors. Black outlines represent emission factors based solely on [7], and light grey from [14]. Dotted outlined represents emission factors based upon the two aforementioned independent studies.



^a Assumed flare gas density: 1.90 kg/m³ (based on flare gas compositions in [8])

^b Assumed flare gas higher heating value: 93 MJ/m³ (as stated in [7])

^c Assumed heating value of 45 MJ/m³ (as stated in CAPP documentation[9])

^d Assumed flare gas density: 0.83 kg/m³ (back-calculated from [9] and [7] with given unit conversions)

^e Assumed flare gas density: 0.85 kg/m³

Figure 1. Sources of available NO_x emission factors converted units of kg NO_x per kg flare gas

1.2 NO_x Scaling Laws

Rokke et al. [16] scaled an emission index (yield of NO_x multiplied by a factor of exit velocity, density, and burner diameter) with the Froude number (defined as $Fr = u_0^2/gd_0$ where the subscript '0' denotes properties at the burner exit, u is the velocity of the gas, d is the diameter of the burner, and g acceleration due to gravity). This relation presented in eq. (1) and was derived with a 15-step reduced mechanism for NO formation via thermal, prompt, and nitrous oxide routes [16]. Noting the common terms on each side of eq. (1), this scaling law reduces to a simple non-linear function of NO_x mass emission rate, \dot{m}_{NO_x} [g/s], with volume flow rate of flare gas, Q [m³/s], as shown in eq. (2).

$$Y_{NO_x} \left(\rho_0 \frac{u_0}{d_0} \right) \approx 44 \left(\frac{u_0^2}{gd_0} \right)^{3/5} \quad (1)$$

$$\dot{m}_{NO_x} \approx 0.047Q^{1.2} \quad (2)$$

where Y_{NO_x} is NO_x yield in [g NO_x/kg flare gas], ρ_0 is the density at the burner exit in [kg/m³], \dot{m}_{NO_x} is the mass emission rate of NO_x in [g/s], and Q is the volume flow rate of flare gas in [10³ m³/s]. Data in the present study will be compared to the scaling relation of eq. (2) derived from [16], and a the simple emission factors presented above.

2. Experimental Setup and Experimental Methods

Experiments were performed at the Carleton University Lab-Scale Flare (CLSF) facility at which custom hydrocarbon and inert fuel mixtures can be flared at up 400 SLPM. Figure 2 shows the burner which sits in a 1.9 m deep concrete pit. Two concentric settling screens and additional air supply vents surround the burner to reduce disturbances to the flame. Centred 3.14 m above the flame, a large fume hood captures combustion product species and dilution air. Samples are collected 10 m downstream where gas- and solid-phase combustion product analysis equipment

continuously monitor concentrations of carbon dioxide, carbon monoxide, nitrogen oxides, methane, acetylene, additional higher hydrocarbons (C2+), and soot. Emission yields are calculated as in [17].

Tests conducted for this report examine three potential variables affecting NO_x yields: fuel chemistry, flow rate, and burner diameter. Pure methane and propane were flared at three flowrates each at a single burner diameter. A hydrocarbon mixture (heavy-4) of 74.54% methane, 15.47% ethane, 6.83% propane, and 3.16% butane was flared at three flowrates each for three burner diameters. The composition of this mixture is based on [18] – a study of flare gas composition in western Canada. Table 1 below summarizes the experiments performed.

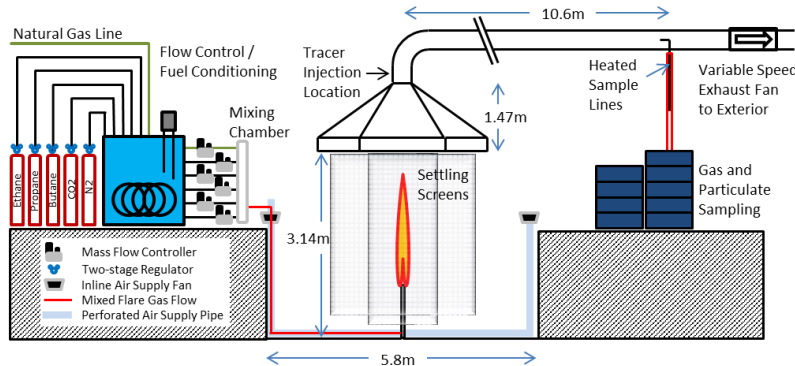


Table 1. Experimental Matrix

Burner Ø [mm]	Fuel Type and Flow Rate [SLPM]		
	Methane	Propane	Heavy-4
38.1			61.56
			102.61
			150.49
50.8	60.80	12.16	60.80
	109.45	30.40	109.45
	182.41	60.80	182.41
76.2			27.36
			68.41
			136.81

Figure 2. Carleton Lab-Scale Flare Facility

3. Results and Discussion

Figure 3(a)-(c) presents the experimental results of NO_x yield on three bases: mass, volume, and energy. Overlaid on the data are lines representing the emission factors previously discussed in their respective published units. Examining Figure 3(a), the data appear to be separated by fuel chemistry by as much as 18% from the average: a linear fit to methane data produces a slope of 0.0017 kg NO_x per kg fuel ($R^2 = 0.998$); propane, a slope of 0.0013 kg NO_x per kg fuel ($R^2 = 0.996$), and combining results of all burner diameters, heavy-4 fit a slope of 0.0016 kg NO_x per kg flare gas ($R^2 = 0.990$). Less significant differences in slope were seen in flares of heavy-4 fuel of varying burner diameter (~12% from the mean). Relative to the current measured data, NO_x emissions from pure methane flares are underestimated by 24% using the EEA emission factor [11] and by 19% using the E&P emission factor [13].

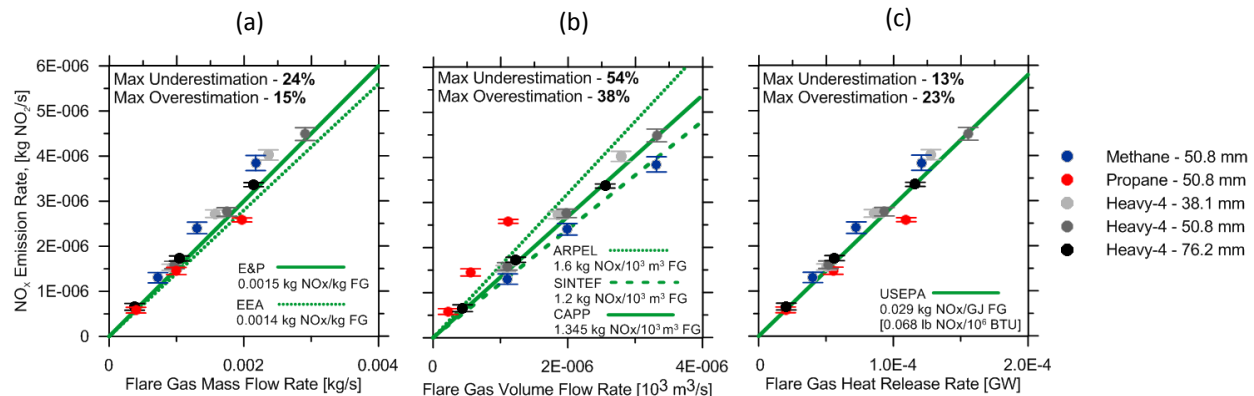


Figure 3. Emission rate of NO_x versus flare gas flow rate in (a) mass, (b) volume, and (c) heat release. Green lines indicate emission factors legislated or suggested by governmental agencies in their published units.

When the data are plotted on a volume basis in Figure 3(b), linear fits for each individual fuel composition are good ($R^2 > 0.99$), but fits for each fuel chemistries have significant differences in slope. The propane data follows a slope of 2.22 kg NO_x per 10³ m³ of flare gas, compared to methane at 1.14 kg NO_x per 10³ m³ of flare gas. The three emission factors discussed that published in mass of NO_x per volume of flare gas (CAPP, ARPEL, and SINTEF [9,10,14]) align well with methane-based fuels, but underestimate NO_x emissions from propane flames by up to 54%.

Data presented in terms of heat release rate in Figure 3(c) appears to slightly collapse the differences in slope due to fuel-chemistry to a maximum deviation of approximately 17% from the mean. The emission factor published by the USEPA [7] aligns with the average slope for all the data – though for the cases examined in this study, the USEPA factor underestimates emissions from methane flares by up to 13%, while overestimating emission from propane flares by up to 23%.

The non-linear relationship between NO_x emission rate and flow rate proposed by [16] is presented in the format of the original publication in Figure 4(a) with data from the present study. Propane data appears to align well with the theoretical scaling law, eq. (1), though methane-based fuels appears to fall below the curve. Figure 4(b) re-plots the proposed scaling relation in mass emission rate of NO_x with volume flow rate and the rearranged scaling law presented in eq. (2). Current emission factors published in volume-based units are also included. It is clear that for the data collected in this study, the appearance of a well-fitting relationship between NO_x emissions and Froude number is perhaps a figment of the common terms and logarithmic scale on both axes of Figure 4(a). Further, comparing this scaling relation to the emission factors, it is clear that the simple power law scaling relation with flow rate does not improve upon the currently utilized linearly scaled emission factors.

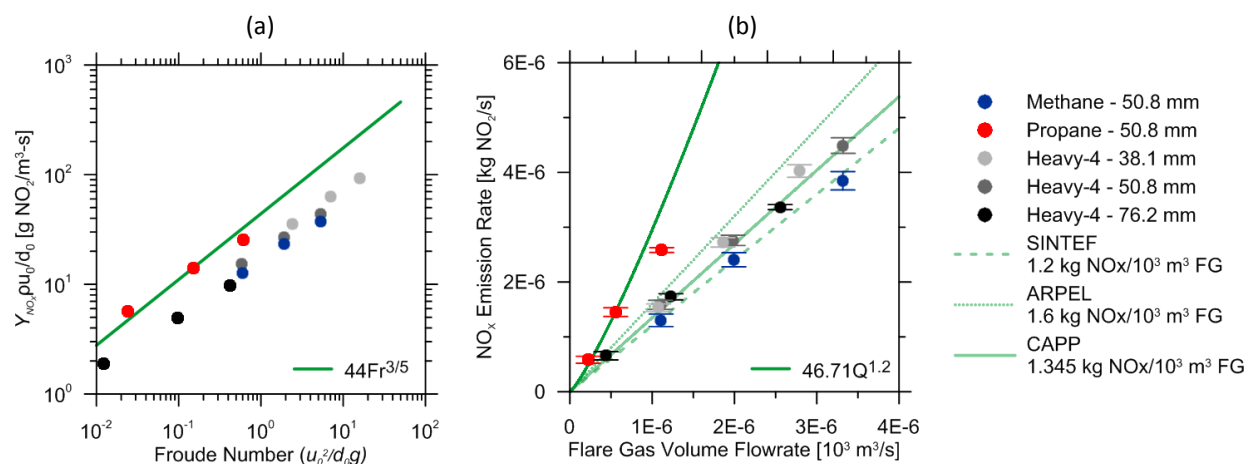


Figure 4. Proposed scaling law of [16] plotted in (a) as presented in original publication and rearranged in (b) in terms of flare gas volume flowrate.

Current emission factors inherently assume a linear relationship between NO_x emission rates and flow rates in volume, mass, or energy basis. It appears that the flowrates and diameters examined, this assumption is reasonable for any one specific fuel mixture. However, the slopes of NO_x emission vs. flares gas flow differ by fuel type leading to significant over and underestimations in NO_x emission estimates. Of the discussed emission factors from various governmental agencies and within the limits of the measured data in the present work, emission factors presented in a mass of NO_x per energy content of fuel best estimates emissions with a maximum error of +12%/-23%. However, a broader range of flare gas mixtures and conditions could be expected to give larger errors. As the thermal mechanism for NO_x is a dominant pathway for formation [19,20], flame temperature and radiant losses due to soot production likely need to play a large part in developing better models for predicting NO_x emissions from turbulent non-premixed flames and flares.

4. Conclusions

NO_x emissions from flares of methane, propane, and natural gas mixtures from 38.1, 50.8, and 76.2 mm burner diameters were examined and compared to current emission factors of agencies in North and South America and Europe. Within the relatively limited data set, NO_x emissions scaled linearly with flare gas flow rate (on a volume-, mass-, and energy-basis) for any one fuel composition; however, no simple relation could predict emissions over a range of different fuels. A proposed scaling law in the literature for a NO_x emission index with Froude number was found to reduce to a simple non-linear relation between NO_x mass emission rate and volume flow rate. This relation predicted NO_x emissions no better than current emission factors within the fuels, flowrates, and diameters examined.

Additional tests to expand ranges flow rate, burner diameter, and fuel chemistry, and consideration of soot formation and flame temperature will significantly aid the pursuit of a robust emission factor for NO_x emissions from flares.

Acknowledgements

Support for this project was provided by the Petroleum Technology Alliance of Canada (PTAC), Natural Resources Canada (Canmet ENERGY-Devon), and Natural Sciences and Engineering Research Council of Canada (NSERC).

References

- [1] C.D. Elvidge, D. Ziskin, K.E. Baugh, B.T. Tuttle, T. Ghosh, D.W. Pack, et al., A Fifteen Year Record of Global Natural Gas Flaring Derived from Satellite Data, *Energies*. 2 (2009) 595–622. doi:10.3390/en20300595.
- [2] BP, Statistical Review of World Energy 2015, 2015. bp.com/statisticalreview.
- [3] U.S. EPA, AP 42 - Compilation of Air Pollutant Emission Factors, Volume I, Section 13.5 Industrial Flares (April 2015), United States Environmental Protection Agency (U.S. EPA), Research Triangle Park, NC, 2015. http://www.epa.gov/ttn/chief/ap42/ch13/final/C13S05_4-20-15.pdf.
- [4] AER, Directive 060: Upstream Petroleum Industry Flaring, Incinerating, and Venting, Alberta Energy Regulator (AER), Calgary, AB, 2014. http://www.aer.ca/documents/directives/Directive060_May2014.pdf.
- [5] N. De Nevers, *Air Pollution Control Engineering*, McGraw-Hill, 1995.
- [6] T.J. Grahame, R. Klemm, R.B. Schlesinger, Public health and components of particulate matter: The changing assessment of black carbon, *J. Air Waste Manage. Assoc.* 64 (2014) 620–660. doi:10.1080/10962247.2014.912692.
- [7] 40 CFR Part 60, Subpart OOOO - Standard of Performance for Crude Oil and Natural Gas Production, Transmission, and Distribution, United States of America, n.d. <https://www.law.cornell.edu/cfr/text/40/part-60/subpart-OOOO>.
- [8] M. McDaniel, Flare efficiency study, United States Environmental Protection Agency, Research Triangle Park, NC, 1983. <http://nepis.epa.gov/Exe/ZyPURL.cgi?Dockey=P1003QGZ.txt>.
- [9] CAPP, A Recommended Approach to Completing the National Pollutant Release Inventory (NPRI) for the Upstream Oil and Gas Industry, 2007. <http://www.capp.ca/library/publications/policyRegulatory/pages/pubInfo.aspx?DocId=119572#a3C7EUiuVHbf>.
- [10] N. Franklin, D.M. Leahey, *Atmospheric Emissions Inventories Methodologies in the Petroleum Industry*, 1998.
- [11] C. Trozzi, 1.B.2.c Venting and flaring, (2013) 1–15.
- [12] R. Villasenor, M. Magdaleno, A. Quintanar, J. Gallardo, M. Lopez, R. Jurado, et al., An air quality emission inventory of offshore operations for the exploration and production of petroleum by the Mexican oil industry, *Atmos. Environ.* 37 (2003) 3713–3729. doi:10.1016/S1352-2310(03)00445-X.
- [13] A. Shah, P. Pope, *Methods for Estimating Atmospheric Emissions from E&P Operations*, The Oil Industry International Exploration & Production Forum, London, UK, 1994. <http://www.epforum.org>.
- [14] J.E. Hustad, M. Jacobsen, N.A. Røkke, *Gas Flaring Analysis: Emissions of non-CO₂-greenhouse gases from flares*, 1992.
- [15] OLF Environmental Programme, Report Phase I, Part A, Emissions to Air, 1991.
- [16] N.A. Rokke, J.E. Hustad, O.K. Sonju, A Study of Partially Premixed Unconfined Propane Flames, *Combust. Flame*. 97 (1994) 88–106.
- [17] D.J. Corbin, M.R. Johnson, Detailed Expressions and Methodologies for Measuring Flare Combustion Efficiency, Species Emission Rates, and Associated Uncertainties, *Ind. Eng. Chem. Res.* 53 (2014) 19359–19369. doi:10.1021/ie502914k.
- [18] J.D.N. McEwen, *Soot Emission Factors from Lab-Scale Flares Burning Solution Gas Mixtures*, M.A.Sc. Thesis, Carleton University, Ottawa, ON, Canada, 2010. <http://proquest.umi.com.proxy.library.carleton.ca/pqdweb?did=2211468981&sid=1&Fmt=6&clientId=13709&RQT=309&VName=PQD>.
- [19] S.R. Turns, *An Introduction to Combustion: Concepts and Applications*, 2nd ed., McGraw-Hill, USA, 2000.
- [20] N.A. Rokke, J.E. Hustad, O.K. Sonju, F.A. Williams, Scaling of Nitric Oxide Emissions from Buoyancy-Dominated Hydrocarbon Turbulent-Jet Diffusion Flames, *Proc. Combust. Inst.* 24 (1992) 385–393.